

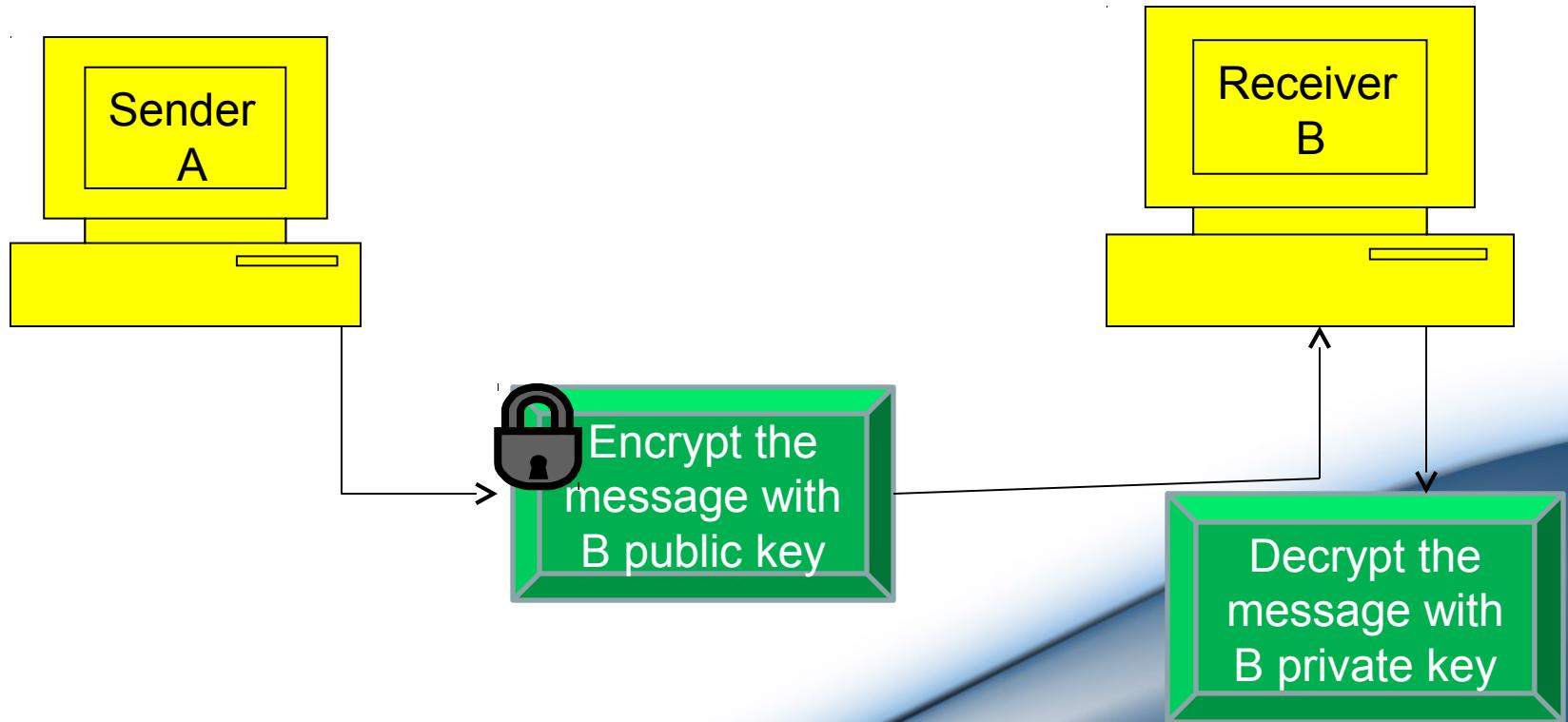
Network Security

Unit-III

ASymmetric Key Algorithms



Overview of asymmetric –key cryptography



One key is used for **locking**. Other is used for **unlocking**.
Public key is used for locking. **Private key** is used for
unlocking.

RSA Algorithm

- Invented by Rivest, Shamir & Adleman of MIT in 1977
- Choose two large prime numbers P and Q
- Calculate $N=P \times Q$
- Select Public key E as not a factor of $(P-1) \times (Q-1)$
- Select Private key D as $(D \times E) \bmod (P-1) \times (Q-1) = 1$
- For Encryption, $CT = PT^E \bmod N$
- Send CT to the receiver
- For Decryption, $PT = CT^D \bmod N$

Example:

- P=7 and Q=17
- Calculate N=7x17=119
- Select Public key E as not a factor of $(P-1)x(Q-1)$ i.e.
- $(7-1)x(17-1) = 6x16 = 96.$
- The factors of 96 are: 2,3,4,15,6.
- So, let us say, we keep E = 5
- Select Private key D as $(DxE) \text{ mod } (P-1)x(Q-1)=1$
- $(Dx5) \text{ mod } (7-1)x(17-1)=1$
- $(Dx5) \text{ mod } 6x16=1.$
- After some calculations, we say D=77
- For Encryption, $CT=PT^E \text{ mod } N$. let us say PT=10
- $CT=10^5 \text{ mod } 119 = 40$
- Send CT to the receiver
- For Decryption, $PT=CT^D \text{ mod } N$
- $PT= 40^{77} \text{ mod } 119 = 10$

Elgamal Cryptography

- The **EIGamal encryption system** is an **asymmetric key encryption algorithm** for public-key cryptography **which is based on the Diffie-Hellman Exchange Agreement.**
- The system parameters consist of a **prime p** and an **integer g** , whose powers modulo p generate a large number of elements, as in Diffie-Hellman.
- A has a **private key a** and a **public key y** , where $y = g^a \pmod{p}$.
- Suppose B wishes to send a message **m** to A. B first generates a **random number k less than p** .
- He then computes :-

$$y_1 = g^k \pmod{p} \text{ and } y_2 = m \text{ xor } y^k,$$

B sends (y_1, y_2) to A.

Upon receiving the ciphertext,

A computes :-

- $m = (y_1^a \pmod{p}) \text{ xor } y_2$.

Elliptic curve algorithm

- Elliptical curve cryptography (ECC) is a **public key encryption** technique based on ***elliptic curve theory*** that can be used to create faster, smaller, and more efficient cryptographic keys.
- ECC generates keys through the **properties of the elliptic curve equation** instead of the traditional method of generation as the product of very large prime numbers.

- ECC was introduced by Victor Miller and Neal Koblitz in 1985.
- It's new approach to Public key cryptography.
- ECC requires significantly smaller key size with same level of security.
- Benefits of having smaller key sizes : faster computations, need less storage space.
- ECC ideal for : Pagers ; PDAs ; Cellular Phones ; Smart Cards.

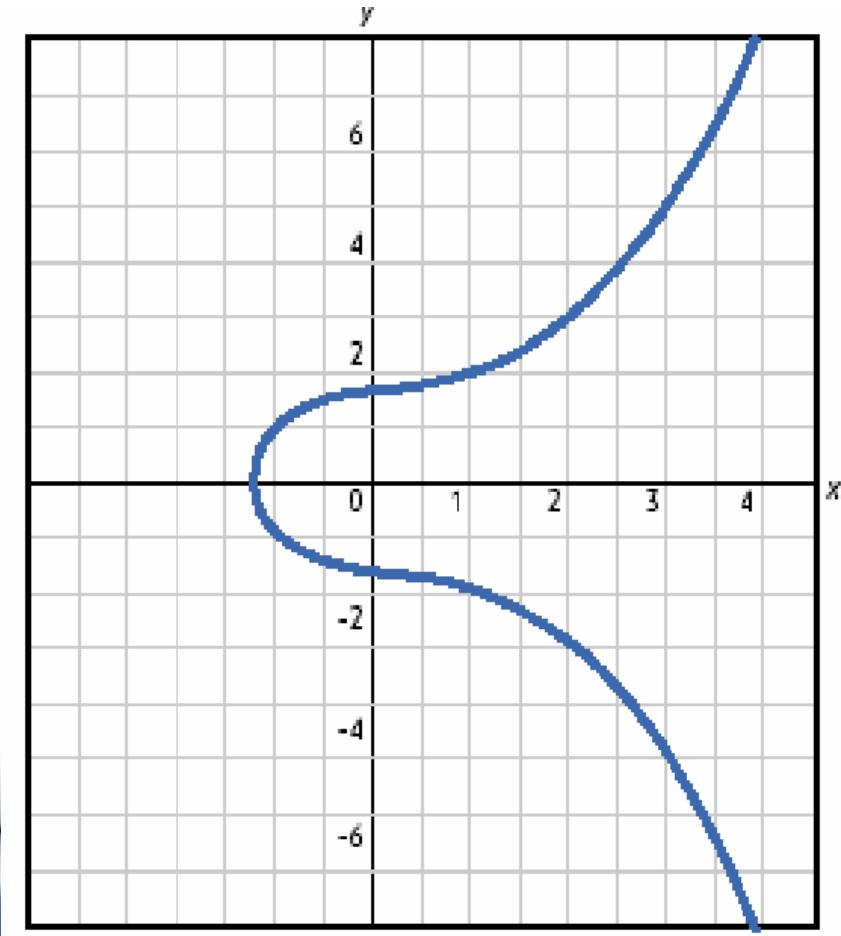
Elliptic Curves

- Standard Form Equation

$$y^2 = x^3 + a.x + b$$

where x , y , a and b are real numbers.

- x, y, a form the **public key** whereas **b** forms a **private key**.



KNAPSACK ALGORITHM

- That is, if M_1, M_2, \dots, M_n are the given values and S is the sum, find out b_i so that:
- $S = b_1M_1 + b_2M_2 + \dots + b_nM_n$
- Each b_i can be 0 or 1.
- 1 indicates that the item is in the knapsack
- 0 indicates that it is not

Plain text	0 1 1 0 1 1	1 1 1 0 0 0	0 1 0 1 1 0
Knapsack	1 7 8 12 14 20	1 7 8 12 14 20	1 7 8 12 14 20
Cipher text	$7 + 8 + 14 + 20 = 49$	$1 + 7 + 8 = 16$	$7 + 12 + 14 = 33$

Message Digest

- A message digest is a **fingerprint or the summary** of a message.
- It is used to verify the **integrity of data** to ensure that the data is not altered in any way.

MD5

- Steps:
 - 1.) Padding (64 bits less than a multiple of 512)
 - 2.) Append Length (of length 64 bits)
 - 3.) Divide the input into 512-bit blocks
 - 4.) Initialize chaining variables
 - 5.) Process Blocks
 - 5.1> copying chaining variables into temporary variables
 - 5.2> Divide current 512 block into 16 subblocks of 32-bit
 - 5.3> perform 4 rounds

Chaining variables :-

word A: 01 23 45 67

word B: 89 ab cd ef

word C: fe dc ba 98

word D: 76 54 32 10

Each of A, B, C, D is a 32-bit register.

Functions used in 4 rounds:-

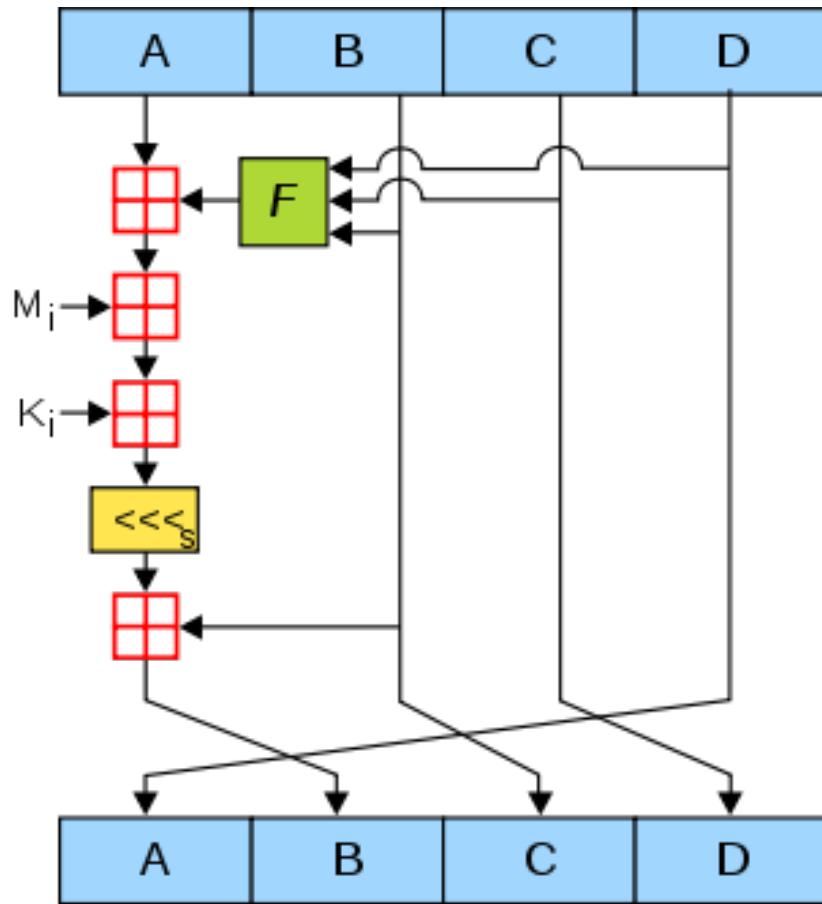
$$F(X,Y,Z) = (X \& Y) \mid (\sim(X) \& Z)$$

$$G(X,Y,Z) = (X \& Z) \mid (Y \& \sim(Z))$$

$$H(X,Y,Z) = X \wedge Y \wedge Z$$

$$I(X,Y,Z) = Y \wedge (X \mid \sim(Z))$$

Four functions will be defined such that each function takes an input of three 32-bit words and produces a 32-bit word output.



A mathematical expression of a single MD5 operation:
 $a = b + ((a + F(b, c, d) + X[k] + T[i]) <<< s)$.

Secure Hash Algorithm (SHA)

- SHA works with any input message that is less than 2^{64} bits in length.
- *The output of SHA is a message digest, which is 160 bits in length (32 bits more than the message digest produced by MD5).*
- *The word Secure in SHA was decided based on two features. SHA is designed to be computationally infeasible to*
 - obtain the original message, given its message digest, and
 - find two messages producing the same message digest.

The Working of SHA

Step 1: Padding : such a way that the length of the message is 64 bits short of a multiple of 512

Step 2: Append Length: appended to the end of the padding as a 64-bit block

Step 3: Divide the Input into 512-bit Blocks: each of length 512 bits

Step 4: Initialize Chaining Variables: five *chaining variables A through E* are *initialized*

Step 5: Process Blocks:

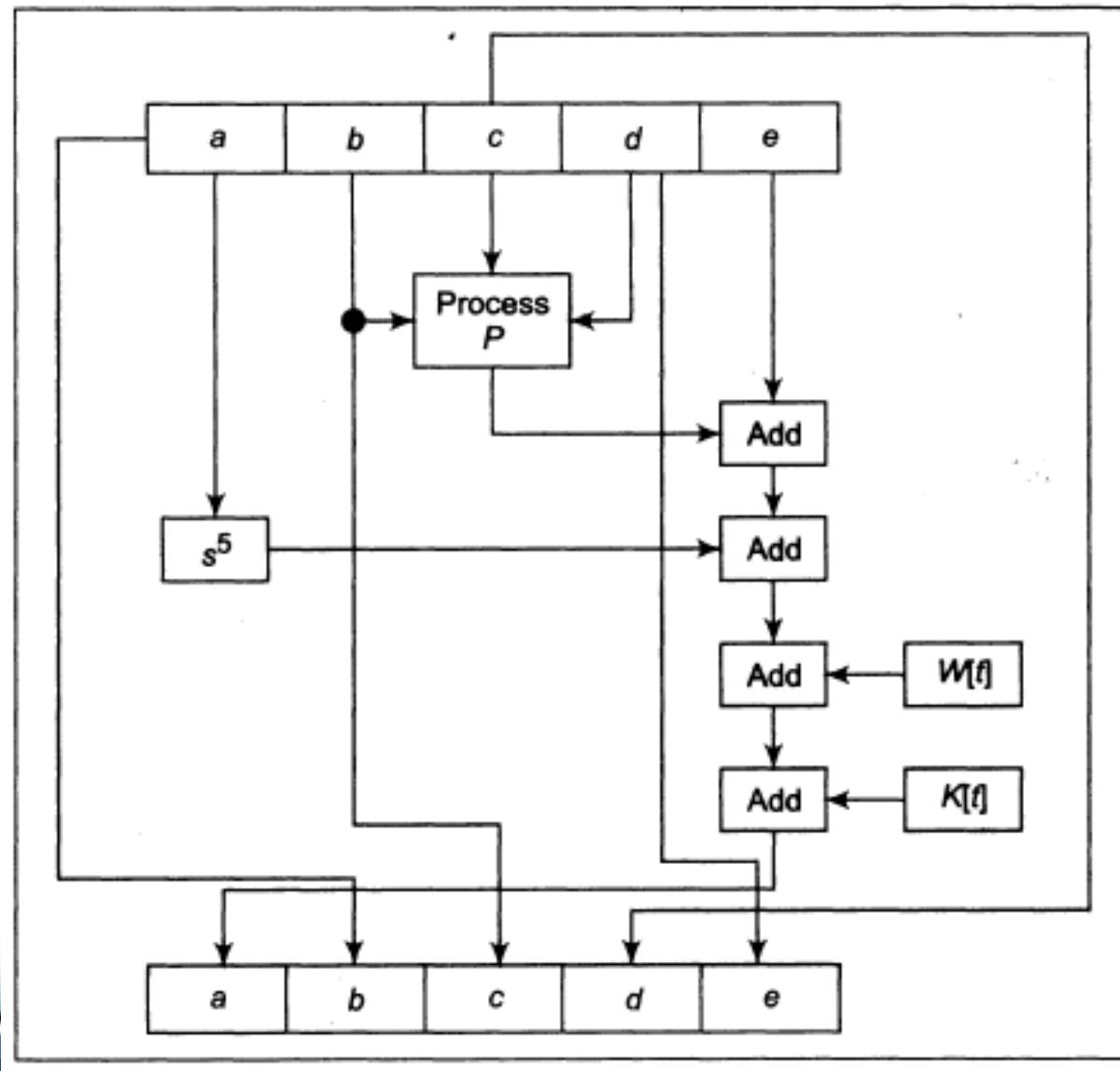
Step 5.1 Copy the chaining variables A-E into variables a-e.

Step 5.2 Now, divide the current 512-bit block into 16 sub-blocks, each consisting of 32 bits.

Step 5.3 SHA has four rounds, each round consisting of 20 steps.

Each round takes the current 512-bit block, the register abcde and a constant K[t] (where t = 0 to 79) as the three inputs.

Single SHA-1 iteration



Mathematically, an iteration consists of the following operations:

$$abcde = (e + \text{Process } P + s5(a) + W[t] + K[t]), a, s30(b), c, d$$

where,

abcde = The register made up of the five variables a, b, c, and e

Process P =

Round	Process P
1	(b AND c) OR ((NOT b) AND (d))
2	B XOR c XOR d
3	(b AND c) OR (b AND D) OR (c AND d)
4	B XOR c XOR d

st = Circular-left shift of the 32-bit sub-block by t bits

W[t] = A 32-bit derived from the current 32-bit sub-block,

first 16 words of W (i.e. t = 0 to 15), the contents of the input message sub-block M[t] become the contents of W[t] straightaway

W[t] = s1 (W [t - 16] XOR W[t - 14] XOR W[t - 8] XOR W[t - 3])

s1 indicates a circular-left shift BY 1 bit

K[t] = One of the five additive constants

SHA-512

The SHA-512 algorithm takes a message of length 2128 bits, and produces a message digest of size 512 bits. The input is divided into blocks of size 1024 bits each.

Step 1: Padding : Like MD5 and SHA-1, the first step in SHA is to add padding to the end of the original message

Step 2: Append Length : length of the message is exactly a multiple of 1024 bits

Step 3: Divide the Input into 1024-bit Blocks

Step 4: Initialize Chaining Variables : Now, eight *chaining variables*, *a* through *h*, are *initialized*.

A = 6AQ9E661F3BCC908	B = BB67AE85S4CAA73B
C = 3C6EF372FE94F82B	D = A54FF53A5F1D36F1
E = 51QE521FADE6B2D1	F -9B05688C2B3E6C1F
G = 1F83D9ABFB41BD6B	H = 5BE0CD19131E2H9

Step 5: Process Blocks

Step 5.1 Copy the chaining variables *A-H* into variables *a-h*. The combination of *a-h*, called *abcdefgfh*

Step 5.2 Now, divide the current 1024-bit block into 16 sub-blocks, each consisting of 64 bits.

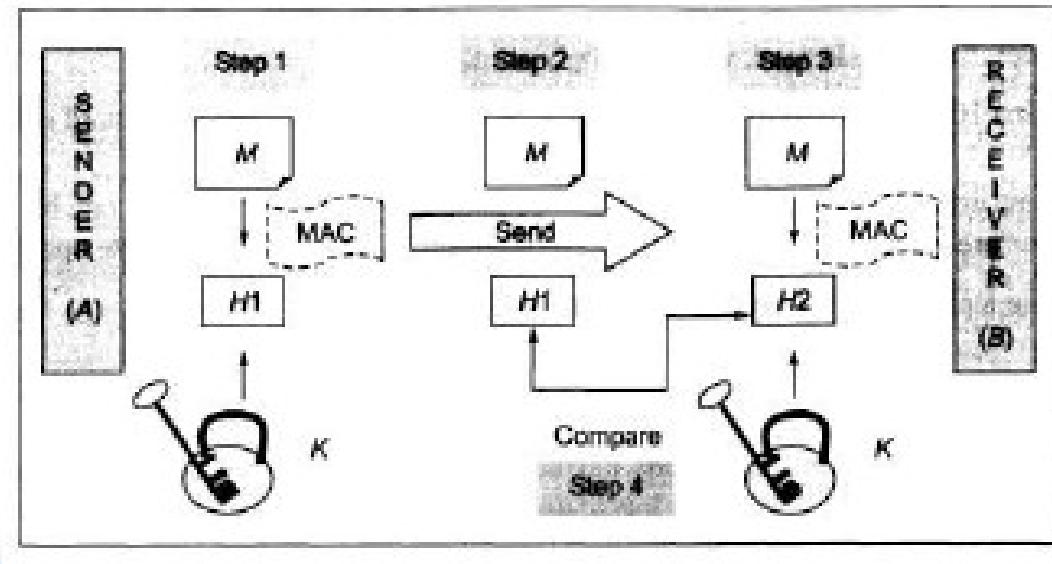
Step 5.3 SHA-512 has 80 rounds. Each round takes the current 1024-bit block, the register *abcdefgfh* and a constant *K[t]* (where *t* = 0 to 79) as the three inputs.

Message Authentication Code (MAC)

The concept of **Message Authentication Code (MAC)** is quite similar to that of a **message digest**. However, there is one difference. As we have seen, a message digest is simply a fingerprint of a message.

There is no cryptographic process involved in the case of message digests.

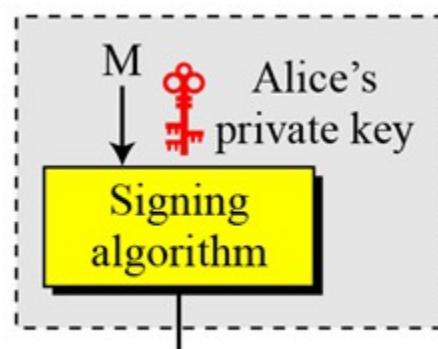
In contrast, a MAC requires that the sender and the receiver should know a shared symmetric (secret) key, which is used in the preparation of the MAC. Thus, MAC involves cryptographic processing.



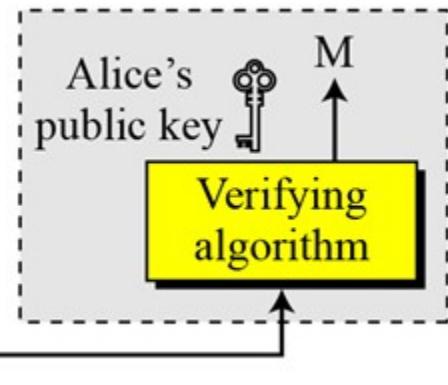
Digital Signature

- To provide **Authenticity, Integrity and Non -repudiation** to electronic documents
- A digital signature is an **electronic signature** that can be used to authenticate the identity of the sender of a message or the signer of a document, and possibly to ensure that the **original content of the message or document that has been sent is unchanged.**
- Digital signatures are **easily transportable**, cannot be imitated by someone else, and **can be automatically time-stamped**

Alice



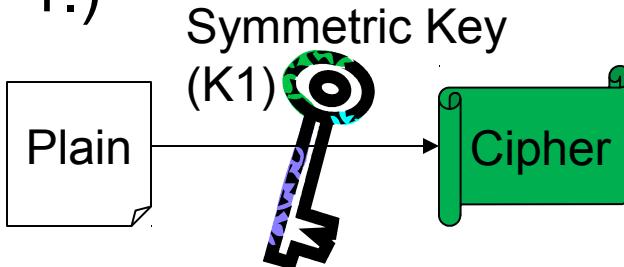
Bob



Symmetry and Asymmetry key together

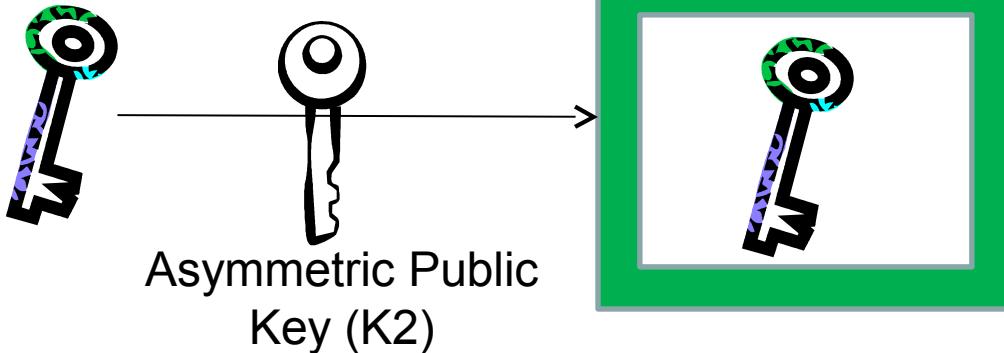
- In practice, symmetric & asymmetric key cryptography are combined to have a very efficient security solution.

1.)



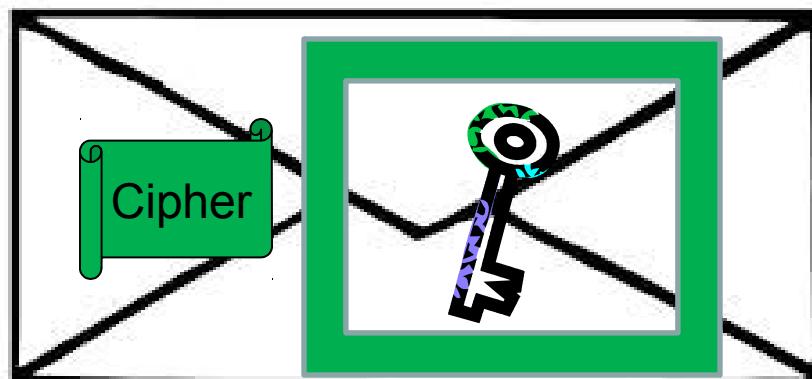
Sender's side

2.)



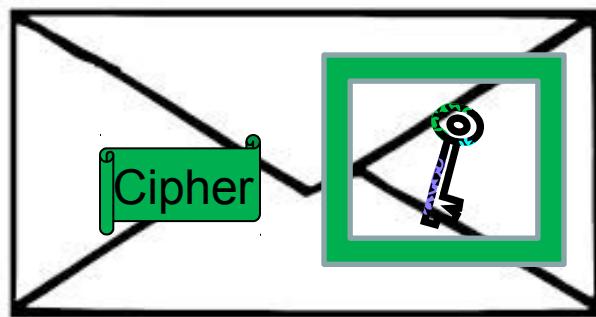
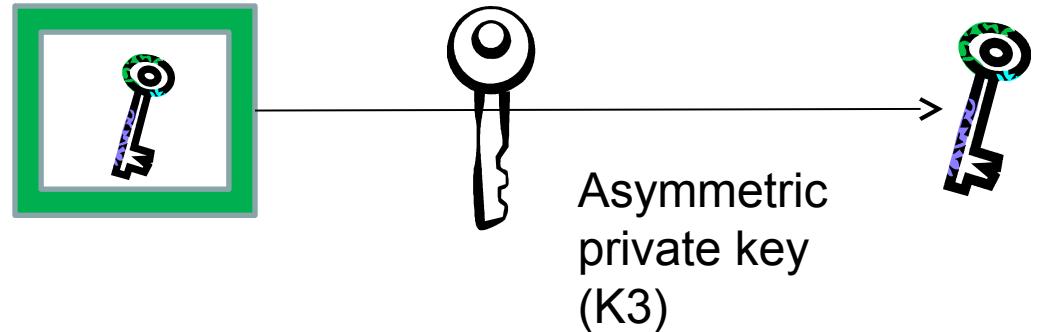
This process is called as "**Key Wrapping**"

3.)

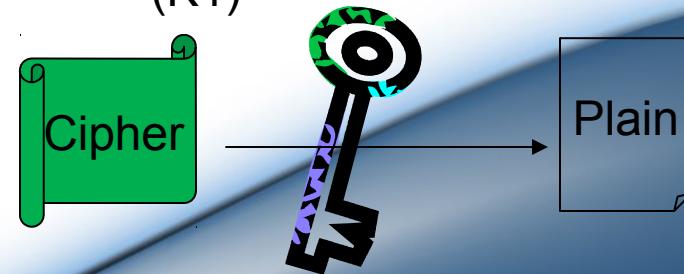


This is called as **Digital Envelope**

Receiver's side



Symmetric key
(K1)



Problems with public key exchange



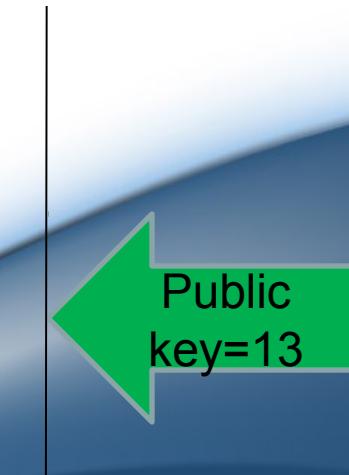
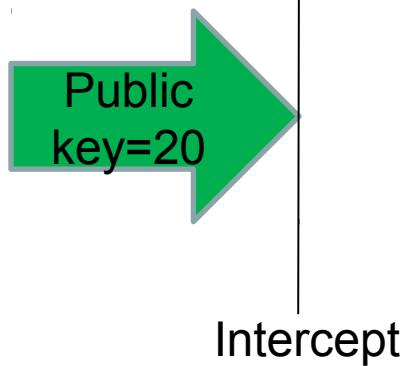
Alice
Public key = 17



Tom
 $A=20, B=13$



Bob
Public key=17



Thank You

